

Simulation of a High-Lift Configuration Embedded with Fluidic Actuators Using PowerFLOW Code

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Abstract

Numerical simulations have been performed for a vertical tail configuration with deflected rudder. The suction surface of the main element of this configuration is embedded with an array of 32 fluidic actuators that produce oscillating sweeping jets. Such oscillating jets have been found to be very effective for flow control applications in the past. In the current paper, a high-fidelity computational fluid dynamics (CFD) code known as the PowerFLOW[®] code is used to simulate the entire flow field associated with this configuration, including the flow inside the actuators. The computed results for the surface pressure and integrated forces compare favorably with measured data. In addition, numerical solutions predict the correct trends in forces with active flow control compared to the no control case. Effect of varying yaw and rudder deflection angles are also presented. In addition, computations have been performed at a higher Reynolds number to assess the performance of fluidic actuators at flight conditions. Unsteady characteristics of oscillatory micro-jets issued from these actuators are also analyzed in this paper.

1. INTRODUCTION

There has been a growing emphasis on reducing the fuel burn of commercial aircraft to meet the stringent restrictions on emissions and noise imposed by regulatory agencies. Improving the fuel efficiency of aircraft will help in reducing the emissions, as well as the direct operating costs of airplanes, a long term goal for commercial companies and airlines. A significant effort is being devoted to reduce the noise and fuel burn through research activities at NASA in the Environmentally Responsible Aviation (ERA) program. One area of research under this program is to increase the lift/drag ratio and/or to reduce the size of control surfaces on aircraft by making use of active flow control (AFC) devices, which will decrease the overall weight and fuel burn of the aircraft, and hence reduce the emissions for a given payload. The AFC devices have to be designed to maximize performance with the least amount of weight penalty and power requirements. In addition, these devices must have acceptable fault tolerance.

Recent advances in computational fluid dynamics (CFD) methods have made it possible to simulate the effect of AFC devices on major aircraft components, as evidenced by a series of publications in the literature [1–5]. The paper of Collis et al. [4] summarizes the various issues encountered in active flow control applications from both theoretical and experimental points of view. In most of these studies, flow control was achieved primarily with synthetic or pulsed-jet actuators. These type of devices invariably consist of moving parts and controllers resulting in increased complexity, which in turn can cause operational problems in flight.

Seifert [6] examined the characteristics and operational mechanism of several different type of actuators, and suggested criteria for comparing their efficiencies. In subsequent papers, Seifert and his

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co-workers [7–9] demonstrated the usefulness of AFC devices for reducing separation and drag on different vehicles, and found the suction and oscillatory blowing actuators to be better suited for their applications.

Rathay et al. [10, 11] have demonstrated performance enhancement of a vertical stabilizer using synthetic jet (zero net mass-flux) actuators. Such actuators consist of electrically driven piezo-electric diaphragms that produce oscillating jets. Whereas such devices performed well at low side-slip angles, the currently available synthetic jet actuators may not be able to provide adequate momentum flux required for achieving fully attached flow on rudder at higher side-slip angles [11].

During the last several years, fluidic actuators have been identified as viable flow control devices for improving the aerodynamic performance of high-lift configurations by mitigating separated flow regions. Such devices do not contain any moving parts and rely primarily on the feedback mechanism triggered by the unsteady bi-stable flow inside the actuators, as discussed by Raghu and Raman [12], Raman [13], and Raman et al. [14, 15]. The performance of such actuators for high-lift configurations has been examined in recent years by DeSalvo et al. [16], Wosidlo and Wygnanski [17], and Seele et al. [18]. Based on the available research, the fluidic actuators that produce spanwise oscillating or sweeping jets without using any moving components and external source to induce oscillations, offer a reliable and efficient mechanism for active flow control applications.

In a recent paper, Vatsa et al. [19] used CFD simulations to examine the internal and external flow structures created by fluidic actuators operating in quiescent air. Numerical studies were conducted to quantify the effect of geometric shape changes and input conditions on the performance characteristics of such actuators. The computed solutions were shown to compare well with available experimental data for several configurations. In the current paper, we examine the effect of an array of such fluidic actuators embedded in a vertical tail configuration that has been tested experimentally by Seele et al. [20]. The primary objective here is to explore and assess the reliability of the PowerFLOW® CFD code for simulating the effect of fluidic actuators on such configurations that produce large side force (lift) when the rudder is deflected.

The outline of the paper is as follows. In section 2, the wind tunnel model and test conditions are described. Section 3 and 4 focus on the numerical simulation method and setup, respectively. The numerical results and the comparisons with the wind tunnel measurements are presented in Section 5, with emphasis given to the effect of flow control on steady (time-averaged) loads and pressure distributions. A numerical characterization of the pulsating flow generated by the actuators is also presented in Section 5. Finally, the main outcomes of the present effort and directions for further investigations are summarized in the conclusive Section 6.

2. CONFIGURATION AND TEST CONDITIONS

The configuration under consideration here corresponds to the vertical tail (stabilizer) model tested by Seele et al. [20] at the California Institute of Technology's Lucas Wind Tunnel, [21] shown schematically in Fig. 1. The planform of this configuration resembles a typical transport wing, and therefore, it is also referred to as a wing in this paper. The model is mounted on a turntable near the floor of the wind tunnel, and the wing planform can be seen in this arrangement from side of the wind tunnel test section. The basic section of this model has a NACA 0012 profile. The wing is tapered and has a leading edge sweep of 42 degrees and a 35% chord rudder (flap). It has a semi-span (b) of 1.067 m (3.5 feet) and a mean aerodynamic chord (MAC) of 0.538 m (1.765 feet). We will refer to the wing section up to the hinge line as the main element, and the flap as the rudder for discussion purposes in this paper. In the experimental work of Seele et al. [20], the gap between the main element and the rudder on the pressure side of the model was sealed using a thin tape, and therefore a no-slip, no-injection condition was imposed on the pressure surface in the current simulations.

This model has 32 fluidic actuators embedded on the suction surface of the main element distributed over the entire span such that the actuator exits are situated in front of the rudder leading edge. All of the actuators are identical in size, and spaced 38 mm (1.5 inches) apart in the spanwise direction. These actuators have internally curved geometry, and have been studied experimentally by Seele et al. [20] and Wosidlo and Wygnanski [17], and computationally by Vatsa et al. [19, 22]. The actuator nozzles are rectangular in shape, with a throat height of 1 mm (0.04 inches) and a width of 2 mm (0.08 inches). When supplied with same mass/momentum flux, such internally curved actuators that produce sweeping jets were found to be more efficient for flow control applications compared to angled actuators [23] and steady jets [24, 25]. It is worth mentioning that the amplitude and oscillating

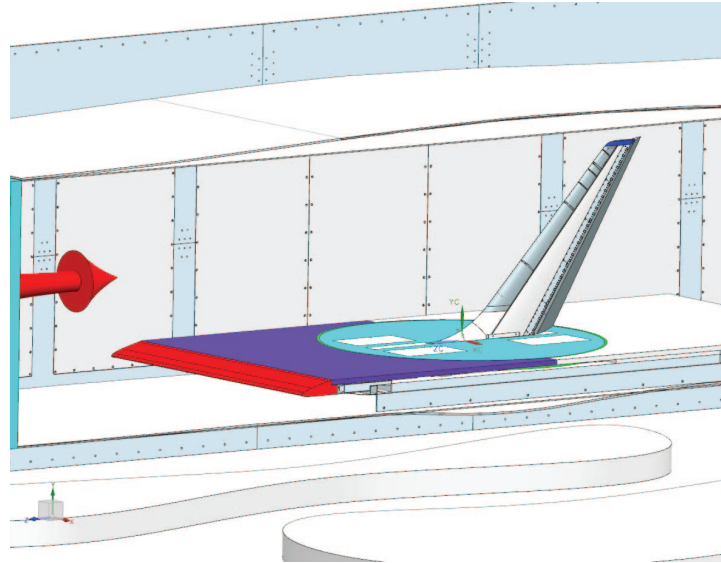


Figure 1. Vertical tail setup in Caltech Lucas wind tunnel.

frequency of the jets produced by such actuators depend primarily on the inlet pressure (or mass flux) and geometric parameters, as documented in the various references quoted earlier in this paper, and no external source is used to induce the spanwise oscillations in these devices.

The fluidic actuators were supplied with compressed air from a feed tube of constant cross-section inserted through the root of the wind tunnel model. The flow rate of air entering the actuators was controlled by an electronic pressure regulator connected to the feed tube. The ejected mass flow was measured by a flow meter. All 32 actuators were located near the trailing edge of the main element. The actuator # 1 is positioned closest to the root section, whereas actuator # 32 is placed near the wing tip. The flow exits the actuators at approximately 10 degree angle relative to the surface of the main element of the vertical tail, and merges with the flow on the rudder's suction surface.

The nominal free-stream velocity in the tunnel is 40 m/sec. To minimize Reynolds number and transition effects for such low speed flows, tripping dots were applied at $x/c = 5\%$ on the suction side, and at $x/c = 10\%$ on the pressure side of the model. Pressure measurements along the chordwise direction are available for this configuration at three different locations corresponding to 40, 70, and 89% span stations of the main element, as shown schematically in Fig. 2. Note that the pressure

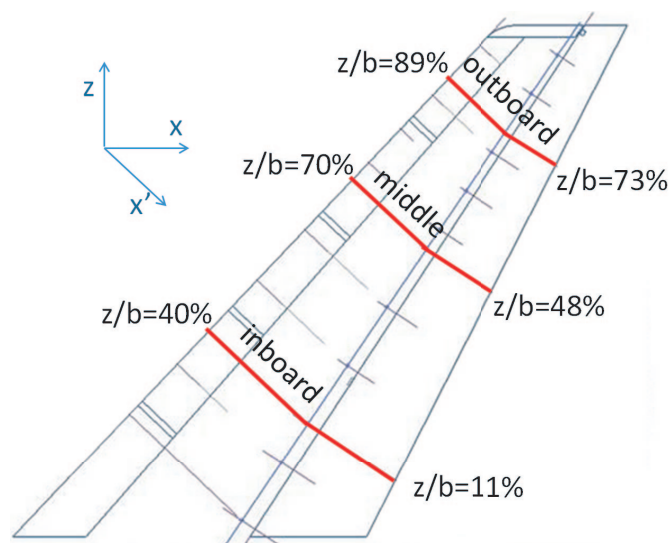


Figure 2. Schematic of chordwise pressure tap rows.

measurements for this configuration are available along lines that are normal to the leading edges of the main element and the rudder sections. Lift (side force) and drag force measurements are also available to quantify the effectiveness of the actuators as control devices for improving the performance of the vertical stabilizer.

3. SIMULATION METHOD

The numerical simulations presented in this paper were performed using the commercial CFD software PowerFLOW® (version 4.4d), which is based on the three dimensional 19 state (D3Q19) lattice Boltzmann model. The lattice Boltzmann model (LBM) can be derived from the velocity space discretization of the general Boltzmann equation, and it recovers the full unsteady Navier-Stokes equations [26–29]. The PowerFLOW® code can be used to solve the lattice Boltzmann equation in a DNS mode, where all of the turbulent scales are spatially and temporally resolved. However, for most engineering problems at high Reynolds numbers, the simulations are usually conducted in conjunction with a hybrid turbulence modeling approach where the small scales are modeled using a modified two-equation $k - \epsilon$ turbulence model and larger, energy-containing scales are directly resolved. The turbulence model uses a swirl correction to locally reduce the influence of the modeled eddy viscosity to allow vortical structures to develop and persist without added artificial damping [30–32]. In addition, a wall model relying on algebraic relations such as the logarithmic law of the wall is used to capture the boundary layer behavior and relax the grid spacing requirement near solid walls [33]. The law of the wall used in this approach has been modified to include pressure gradient effects. The turbulence modeling approach together with the inherently unsteady nature of the LBM ensures accurate and efficient simulation of the large structures, especially in regions of separated flows and shows conceptual similarities with the DDES approach of Spalart et al. [34].

The lattice Boltzmann equation is solved on embedded Cartesian meshes, which are generated automatically within the flow solver for the configuration under consideration, irrespective of the geometric complexity. Variable resolution (VR) regions can be defined to allow for local mesh refinement of the grid by successive factors of two in each direction [35]. The PowerFLOW® code scales well on modern computer clusters consisting of thousands of processors, making it ideally suitable for large scale applications. The LBM methodology used here has been extensively validated for a wide variety of applications ranging from academic cases by using DNS mode [36], to industrial flow problems in the fields of aerodynamics, thermal management, and aeroacoustics, see e.g., Refs. [5, 32, 37–39].

4. COMPUTATIONAL SETUP

The computational setup used in the present study consists of 11 Variable Resolution (VR) levels, numbered from VR0 to VR10. A sketch of the setup is shown in Fig. 3. The simulation domain is enclosed by top, bottom, and side walls where a slip boundary condition is imposed. A viscous, no-slip condition is imposed on the central patch of the bottom wind tunnel wall surrounding the wing root. The upstream size of this viscous wall patch is such that a prescribed value of the boundary layer thickness is achieved at a selected streamwise location. These computational boundaries are used here to approximate the walls of the Caltech Lucas wind tunnel [21]. It should be noted that the region below the mounting plate is ignored in current simulations.

A viscous wall condition is imposed on all of the components that form the vertical stabilizer configuration. The presence of the transition tripping dots at $x/c = 5\%$ and $x/c = 10\%$ on the suction and pressure side of the main element is modeled by prescribing laminar patches, as shown in Fig. 4. Velocity is imposed at the inlet boundary, whereas static pressure is imposed at the outlet boundary. The cross-section of the computational domain is nearly identical to the Caltech Lucas wind tunnel. Some of the VR levels are marked on Figs. 3 and 4 for reference. Several of these VR levels have been obtained by offsetting the surface of the model and by setting some regions around specific parts of the model (tip, leading/trailing edges, fixed/movable gap etc.). The highest VR levels, from VR8 to VR10, are used to model the flow inside the actuators, as shown in Fig. 4. In the no-control case, the VR9 and VR10 in the actuators are reverted to VR8 and the overall number of VR levels is reduced to 9. The minimum voxel (cubic cell) edge length is 3.39×10^{-5} m and 1.35×10^{-4} m for the control and no-control cases, respectively. In the actuated (control) case, 30 grid points (cells) are used along the shortest dimension of any rectangular sectional area along the actuator axis.

Figure 4 shows a global view of the actuation line at the top of the figure, and a detailed view of the VR setup for one of the actuators at the bottom. All the actuators are connected with a single

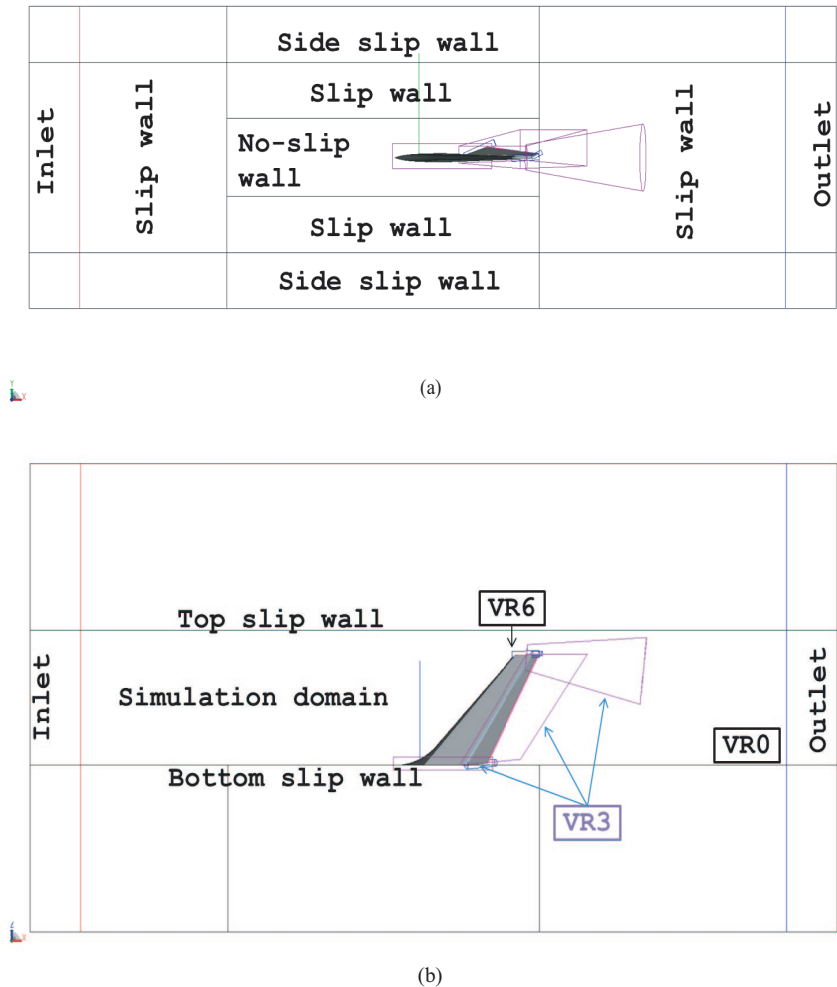


Figure 3. Computational setup. (a) side view (viewed from top of test section) and (b) planform view (viewed from side of test section).

feed tube of rectangular cross section. Mass flow rate is prescribed at the inlet section of the feed tube, close to the root of the stabilizer to replicate the experimental set up. The VR setup inside the actuators is such that the finest resolution level is set in the throat region, where the highest velocities and shear stresses are expected. The outlet of the actuator is in a VR9 level, corresponding to 15 cells along the height of the actuator. The resolution is progressively coarsened from VR10 to VR6 in the feed tube. The coarsest voxel size anywhere in the computational domain is set at 0.035 m for all the cases.

The PowerFLOW[®] code uses explicit time marching to solve the governing equations in a time consistent manner. The solution on a given VR level is updated twice as often when compared to the number of solution updates on the next coarser VR level. Thus, the solution on the finest grid is updated most frequently, whereas the solution on the coarsest grid is updated least often to advance the solution in the whole domain to the same physical time. Comparable number of voxels (cells) on coarser grids are therefore less expensive from the computational point of view. The computational cost to advance the solution to the same physical time for one voxel on a coarse VR level is 1/2 the cost for a voxel on the next finer VR level and so on. In other words, each successive coarser level voxel is equivalent to 1/2 voxels of the next finer grid in terms of computational cost. For book-keeping purposes and estimating the computational resources, we use the appropriate weighting factors to sum up the contributions of the voxels from different VR levels for obtaining a fine-grid equivalent voxel count, starting with a weight factor of unity for the finest grid. The computational cost per time-step is therefore directly proportional to the fine-grid voxel count obtained in this manner.

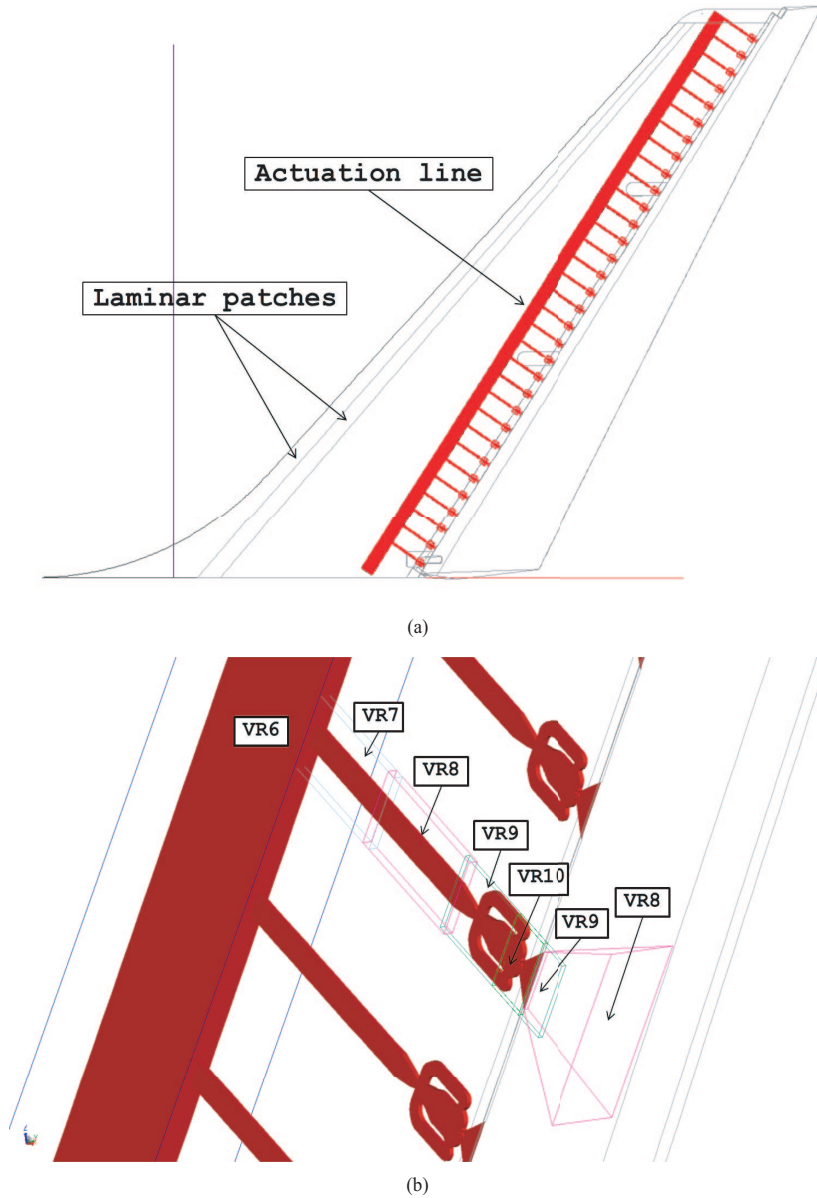


Figure 4. Actuator setup. (a) actuation line and (b) zoomed view of actuators.

5. RESULTS

The computations of the three-dimensional (3-D) flow field for the vertical stabilizer configuration with and without flow control (actuation) have been performed using the PowerFLOW® code. The baseline conditions chosen for this work correspond to zero mass flow (no actuation) at a freestream speed of 40 m/sec and a rudder deflection of 30 degrees. The Reynolds number based on the mean aerodynamic chord is 1.36 million. In addition to the no-actuation case ($C_{mu} = 0$), the experimental data for this configuration is also available for several other values of momentum coefficient. Results from the simulations performed at $C_{mu} = 0$ and 0.5%, corresponding to the experimental study of Seele et al. [20] are presented in this paper. Finally, results showing effect of varying the yaw and rudder deflection angles, as well as the Reynolds number are also included here.

The geometric manipulation and grid generation capability available in the PowerFLOW® software makes it very convenient to conduct parametric studies for complex configurations. For the current configuration, the main element and rudder geometries are imported as individual surfaces. With the available information about the center and axis of rotation, we can easily change the rudder deflection

and yaw angle to match the experimental test conditions. In addition, the grid resolution is easily changed via input parameters and the grids are generated automatically by the software.

5.1. Baseline Configuration, $\delta_R = 30^\circ$, $\beta = 0^\circ$

The baseline configuration here is the vertical tail configuration of Seele et al. [20] with a rudder deflection angle (δ_R) of 30° , and a yaw angle (β) of zero degrees. For the no actuation case ($C_{mu} = 0$) at these geometrical settings, a grid consisting of 441 million voxels distributed among 9 VR regions was used. For the actuated case ($C_{mu} = 0.5\%$), the computational region employed two additional VR regions for a total of 11 VR regions resulting in 643 million voxels. The fine-grid equivalent voxel count, as defined in the previous section, are comparable for these cases. However, the finest cell size and time-step for the actuated case was $\frac{1}{4}th$ compared to the non-actuated case. Therefore, greater number of time-steps are required for the flow-field to settle for the actuated case, resulting in higher computational cost for such cases.

For the actuated cases, the governing equations are solved here to simulate the unsteady flow developing inside the fluidic actuators instead of using approximate surface boundary conditions to simulate the effect of actuators. As observed in Ref. 19, the jet exit velocity and frequency of spanwise oscillations of the exit flow depend primarily on the input mass flow (or gauge pressure) and the geometric details of the actuators. The total mass flow going through the actuators is 0.01433 kg/sec (0.03159 lbm/sec) for $C_{mu} = 0.5\%$.

The computations were run long enough for the integrated forces to settle in time before extracting the surface data. The convergence histories for the drag (C_D), and side force (C_Y) coefficients are shown in Fig. 5. Note that due to the inherent unsteady nature of the flow associated with such configurations, the force coefficients display low level of oscillations even for the non-actuated case after the initial transients are settled. Higher level of oscillations in the force coefficients is observed for the corresponding actuated case due to the presence of bi-stable unsteady flow inside the fluidic actuators. Time-averaging was performed starting at $t = 0.25$ seconds to obtain the force coefficients. The computed values of side force (C_Y), and the drag force (C_D) coefficients are compared with the experimental data of Ref. 20 in Table 1. The simulations predict the correct qualitative trends with actuation, although the increment in side force due to actuation is under-predicted.

To ascertain that the integrated forces reported here for the actuated and non-actuated cases were not affected by differences in grid resolution used for these cases, the computations for the baseline configuration without the presence of actuation (flow control) were repeated on a grid identical to the actuated case, which consisted of 11 VR regions, instead of the original 9 VR regions employed for this case. The resulting value of side force (C_Y) coefficient based on this simulation differed from the

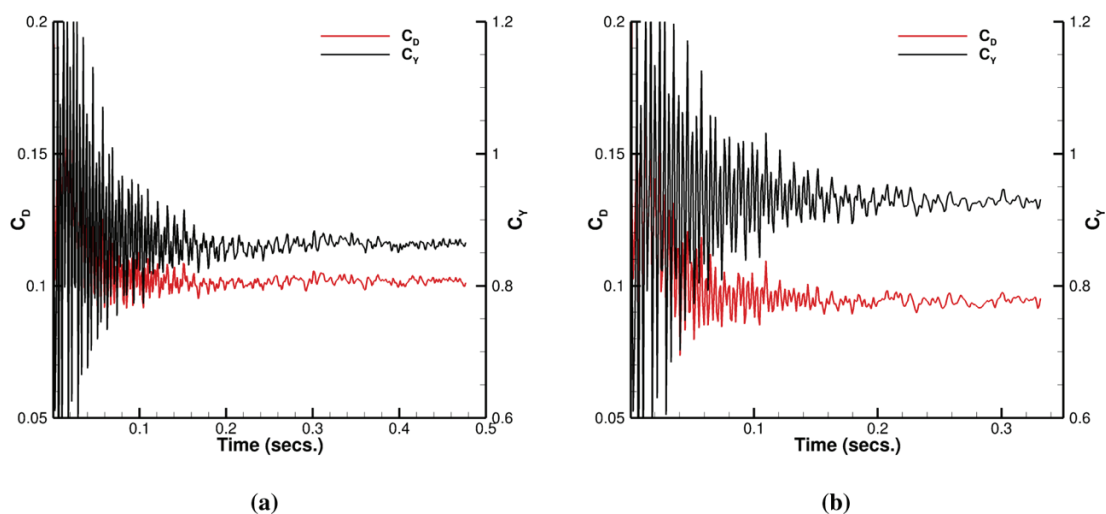


Figure 5. Convergence history of force coefficients for baseline case.

(a) $C_{mu} = 0.0\%$ and (b) $C_{mu} = 0.5\%$.

coarser grid results by 0.03%, whereas the drag force coefficient (C_D) differed by 0.05%. Such difference in results due to grid variation are insignificant from a practical point of view, and the rest of the non-actuated cases were performed on the coarser grids consisting of 9 VR regions for efficiency reasons.

Examination of the velocity field revealed the presence of high subsonic (near sonic) velocities inside the actuators for the $C_{mu} = 0.5\%$ case. Accuracy of the current version of PowerFLOW[®] code (version 4.4d) is known to deteriorate at higher subsonic speeds, and therefore can adversely affect the results of the actuated cases presented here. Effort is currently under way to repeat the actuation cases with a high subsonic (beta) version of the PowerFLOW[®] code.

Pressure coefficient (C_p) contours based on time-averaged simulation data for the actuated and non-actuated cases are shown in Figs. 6 and 7 for the pressure and suction surfaces, respectively. It is apparent from the results presented in Fig. 6 that actuation had very little impact on the pressure distribution on the pressure side of this configuration. However, that is not the case on suction side. A close look at the pressure contours shown in Fig. 7 indicates higher suction pressure levels over most of the suction

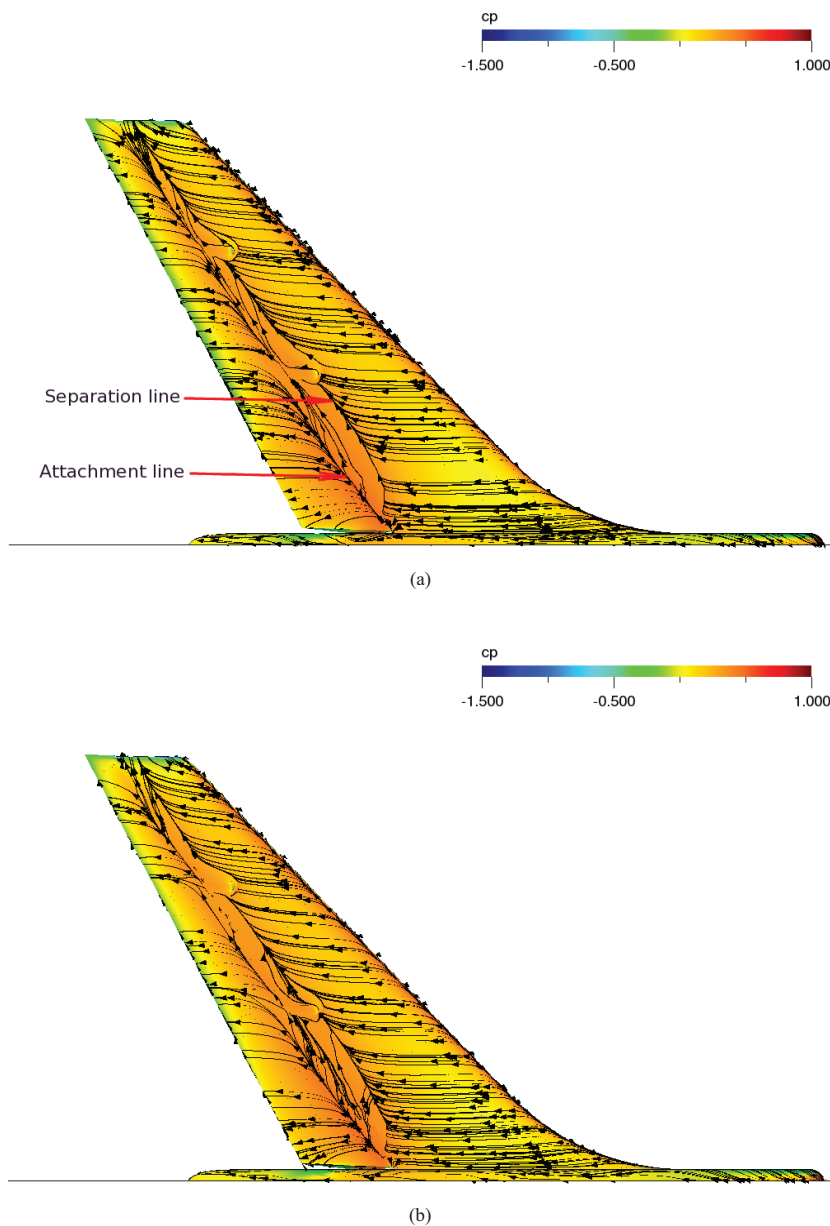


Figure 6. Simulated pressure surface streamline pattern for baseline configuration.

(a) $C_{mu} = 0.0\%$ and (b) $C_{mu} = 0.5\%$.

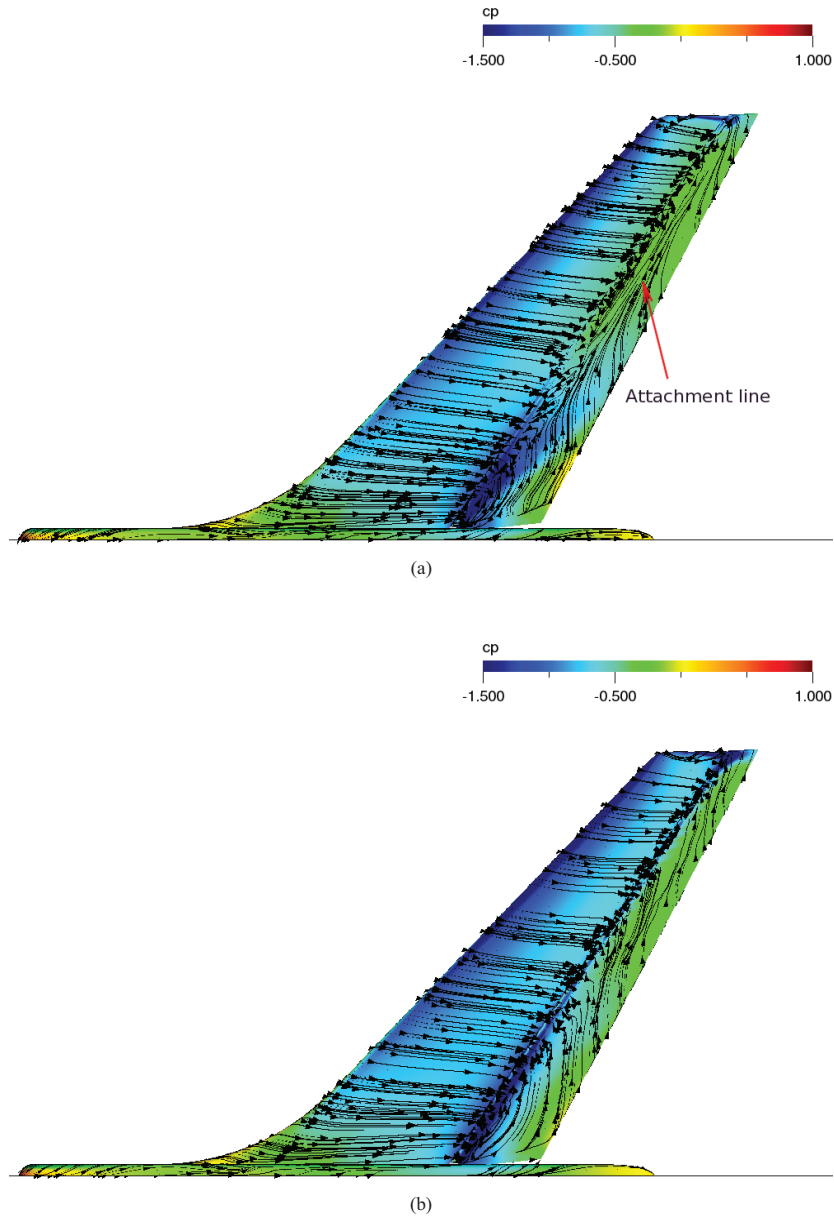


Figure 7. Planform view of simulated suction surface streamlines for baseline configuration.
(a) $C_{mu} = 0.0\%$ and (b) $C_{mu} = 0.5\%$.

surface for the actuated case, which results in higher side force in the presence of actuation. It is believed that actuation increases the overall circulation level, and hence produces higher side force (lift) and suction peaks observed here.

Simulated surface streamline patterns created using time-averaged flow field data are also superimposed over pressure coefficient (C_p) contours in Figs. 6 and 7. The streamline patterns on the pressure side for the actuated and non-actuated cases appear nearly identical in Fig. 6, including the extent of reverse flow region which is delineated by the separation and attachment lines. Such a result is not surprising because the actuator outlets are situated upstream of the suction side of the rudder leading edge, and are practically shielded from the pressure side. However, the flow pattern on the suction surface (see Fig. 7) displays a greater impact of actuation on the rudder, especially downstream of the hinge line. Reverse flow region bounded by the hinge line and a distinctly formed attachment line on the rudder's suction surface is observed in Fig. 7(a) for the non-actuated case. Absence of similar attachment line in Fig. 7 (b) is indicative of reduced reverse flow on the rudder for the actuated case.

The effect of actuation on controlling the extent of separated flow region on the rudder is more obvious from Fig. 8, where cross-sectional view of the simulated streamline pattern near the mid-span section are compared for the actuated and the non-actuated cases. These streamlines are colored with the velocity magnitude. It is clear from the results shown in this figure that the transverse extent of reverse flow region and low velocity regions are reduced in the presence of actuation compared to the baseline (non-actuated) case.

A perspective view from the suction side is also presented in Fig. 9, displaying the streamline pattern in the vicinity of wing root section. The footprint of a corner vortex can also be seen in this figure, although a better view of the vortical flow is seen in Fig. 10, which shows the unconstrained (3-D) streamline pattern that develops above the suction surface. Identical seeding for streamlines was used to generate these figures for the actuated and non-actuated cases. Corner vortex near the wing root, and tip vortex near the wing tip are clearly visible in this figure. It appears that these vortices are more tightly wound for the non-actuated case (Fig. 10 (a)), whereas the vortices for the actuated case (Fig. 10 (b)) appear more diffused and stretched

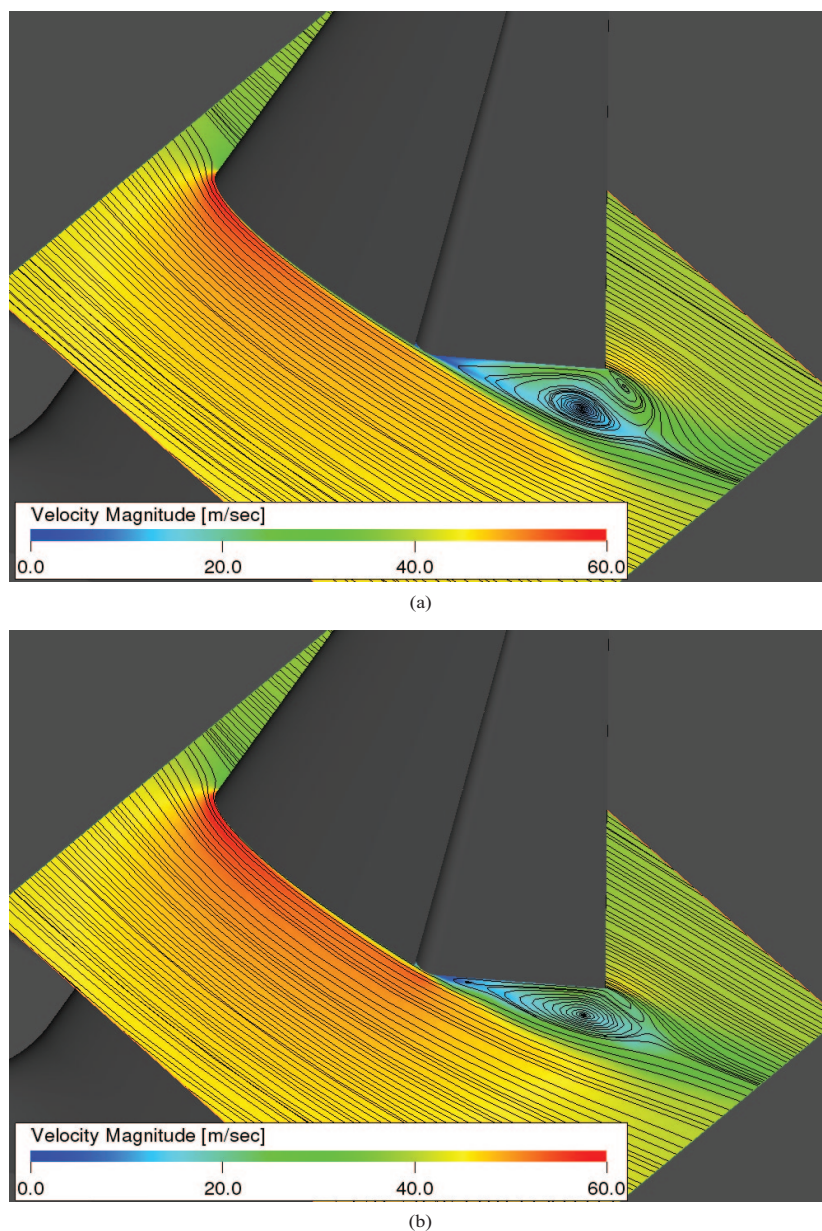


Figure 8. Simulated streamlines near mid-span plane for baseline configuration.

(a) $C_{\mu} = 0.0\%$ and (b) $C_{\mu} = 0.5\%$.

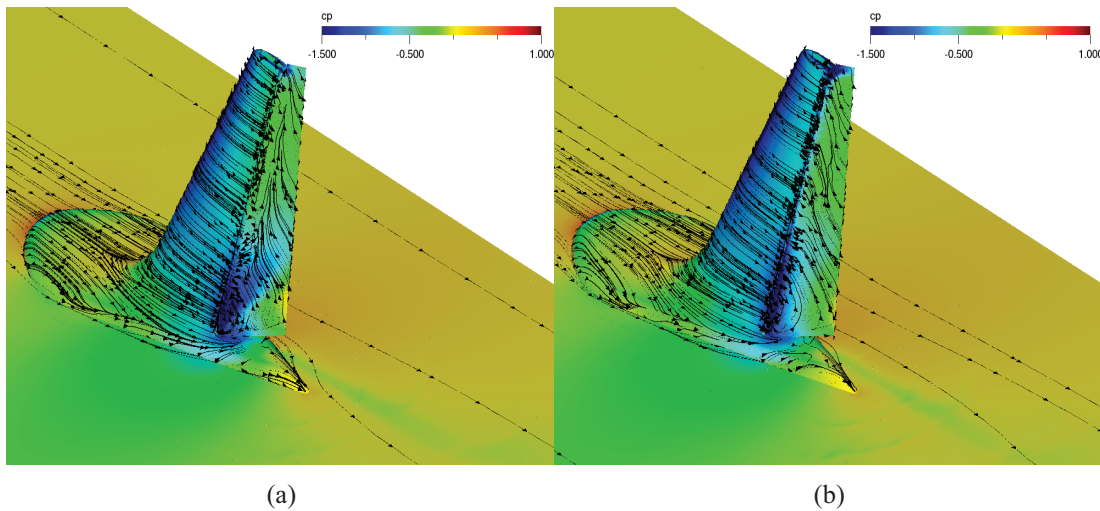


Figure 9. Perspective view of simulated suction surface streamlines for baseline configuration. (a) $C_{mu} = 0.0\%$ and (b) $C_{mu} = 0.5\%$.

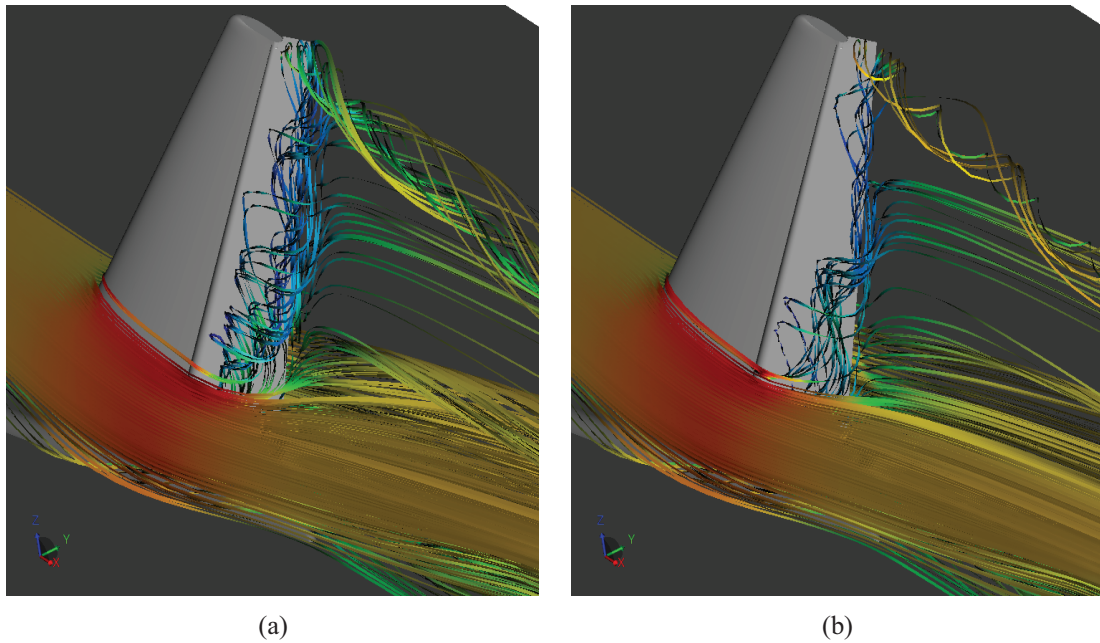


Figure 10. Simulated 3-D streamlines over suction surface for baseline configuration. (a) $C_{mu} = 0.0\%$ and (b) $C_{mu} = 0.5\%$.

out along the span direction. Unfortunately, equivalent flow visualization images from experimental work are not available for comparison with simulated results at this time.

Although the results presented so far are extremely helpful in understanding the overall flow characteristics and the effect of actuation on the flow field for this configuration, these results are mostly qualitative in nature. For quantitative assessment of numerical accuracy of the current simulations, the computed chordwise pressure distributions at three spanwise stations, namely inboard (40%), middle (70%) and outboard (89%) stations (see Fig. 2 for schematic of span locations), are compared with experimental data in Fig. 11. The agreement between the computed and measured pressure distributions for the non-actuated case is quite good, except for the suction surface of the rudder on the inboard station. Although, every effort has been made to model the geometric details of the experimental setup based on the available information, it was impractical to replicate every minute detail of the mounting hardware, especially in the wing root region for the current simulations. There was also some uncertainty

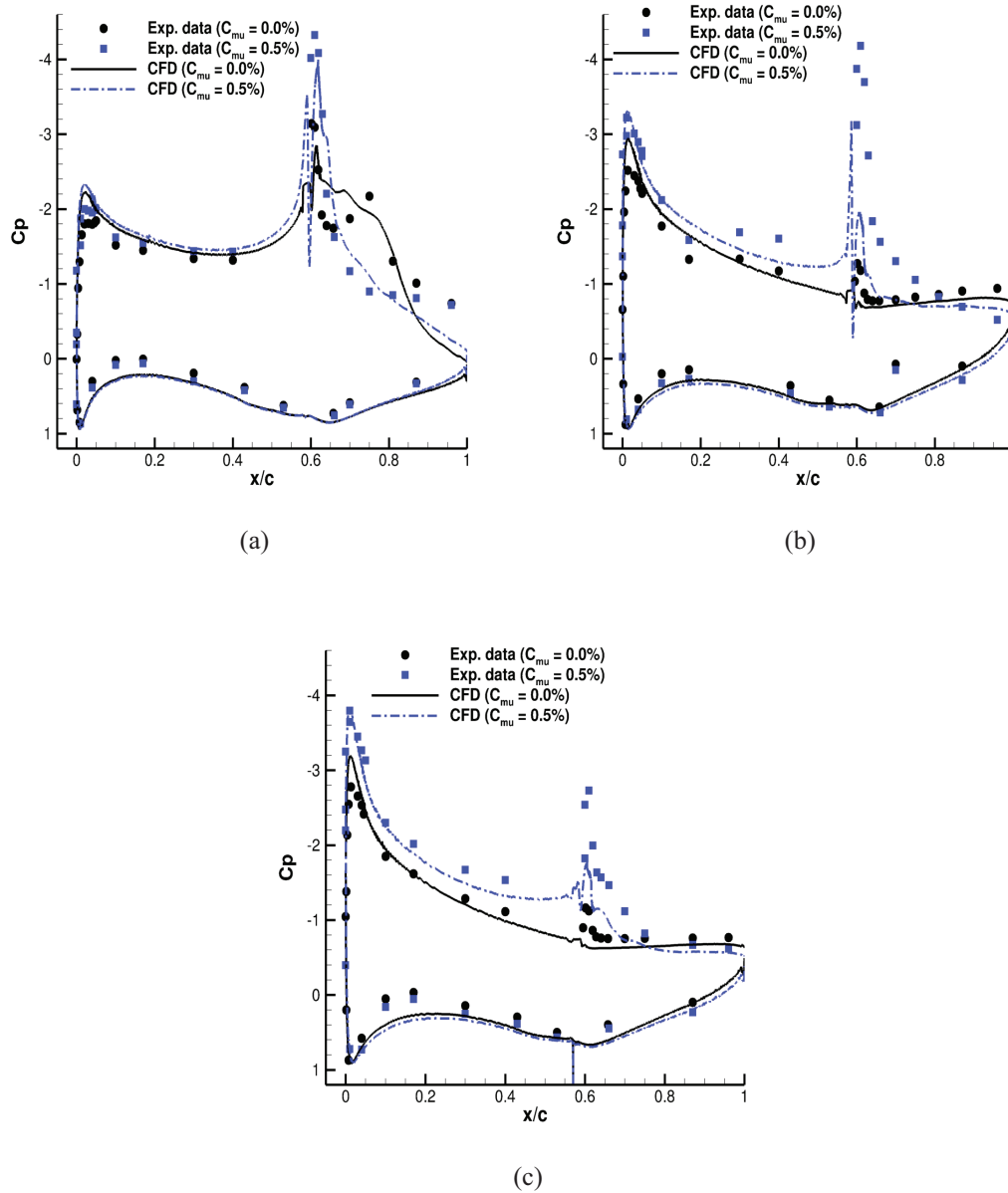


Figure 11. Chordwise surface pressure comparisons: baseline case, $\delta_R = 30^\circ$, $\beta = 0^\circ$.
 (a) inboard, $z/b = 40\%$, (b) middle, $z/b = 70\%$ and (c) outboard, $z/b = 89\%$.

regarding the precise details of a thin gap on the suction surface along the spanwise direction in the vicinity of the rudder hinge line. Such geometrical differences are expected to have most influence on the flow field near the inboard section, and in the vicinity of hinge line. These are precisely the regions where the computed results differ the most from the measured data in Fig. 11.

The pressure distributions obtained for the actuated ($C_{mu} = 0.5\%$) case indicate higher suction pressure levels similar to the ones observed in the experimental data, and the computational results are found to be in good agreement with the measurements over most of the main wing section. The suction peaks are under-predicted in the vicinity of the hinge line, which could be attributed to either slight differences in geometry or lack of resolution in the suction surface gap region along the hinge line. Despite these differences, the computed results predict the correct overall trends in pressure distribution with active flow control using fluidic actuators. The integrated forces extracted from these simulations are compared with the measured data in Table 1. Although the increment in side force due to flow control is under-predicted, the computed results show the correct qualitative trends with actuation.

Table 1. Comparison of force coefficients at wind tunnel Reynolds number

$\delta_R(deg)$	$\beta(deg)$	$C_{mu}(\%)$	$C_Y(exp)$	$C_Y(CFD)$	$C_Y-C_{Y0}(exp)$	$C_Y-C_{Y0}(CFD)$	$C_D(exp)$	$C_D(CFD)$
30.0	0.0	0.0	0.780	0.8540	0.000	0.0000	0.112	0.1019
30.0	0.0	0.5	0.919	0.9273	0.139	0.0733	0.106	0.0942
30.0	7.5	0.0	1.140	1.2784	0.000	0.0000	0.163	0.1690
30.0	7.5	0.5	1.227	1.3042	0.087	0.0258	0.160	0.1543
40.0	0.0	0.0	0.918	1.0134	0.000	0.0000	0.163	0.1591
40.0	0.0	0.5	0.983	1.0471	0.065	0.0337	0.159	0.1556

5.2. Rudder Deflection Angle, $\delta_R = 40^\circ$, $\beta = 0^\circ$

The next configuration under consideration had a value of $\delta_R = 40^\circ$ for the rudder deflection angle compared to the baseline case of $\delta_R = 30^\circ$. The process to set up this case of higher rudder deflection angle was very straight-forward and required changing just one input parameter in the PowerFLOW® case setup of the baseline configuration. Simulations have been performed for these rudder settings at $C_{mu} = 0$ and $C_{mu} = 0.5\%$, corresponding to the momentum coefficients used for the baseline configuration. To expedite the computations, these cases were initiated using solutions from the baseline configuration of $\delta_R = 30^\circ$. As in the previous case, computations were run long enough in time to purge the initial transients out before starting the averaging process on flow solutions and integrated forces.

The time-averaged pressure distributions for the 40° rudder deflection angle at middle and outboard span stations are compared with the baseline case in Figs. 12 and 13, respectively. Results for $C_{mu} = 0$ and $C_{mu} = 0.5\%$ are presented in these figures, along with the results for the baseline configuration of $\delta_R = 30^\circ$ for comparison purposes. The trends observed in the measured data due to increase in rudder deflection angle are replicated by the computational results for both of these cases. For example, the increase in suction peaks in the leading-edge region of the main element with increase in deflection angle are accurately predicted. Another observation worth noting is the relatively flat C_p distribution in the aft region of rudder's suction surface, even with actuation for $\delta_R = 40^\circ$. Such pressure plateaus (also seen in the experimental data) are generally observed in the presence of reverse flow regions. Apparently, actuation with a momentum coefficient of $C_{mu} = 0.5\%$ was not adequate to control the flow separation at the higher rudder deflection angle. The increment in side force with actuation is also under-predicted, as seen from the tabulated results (Table 1).

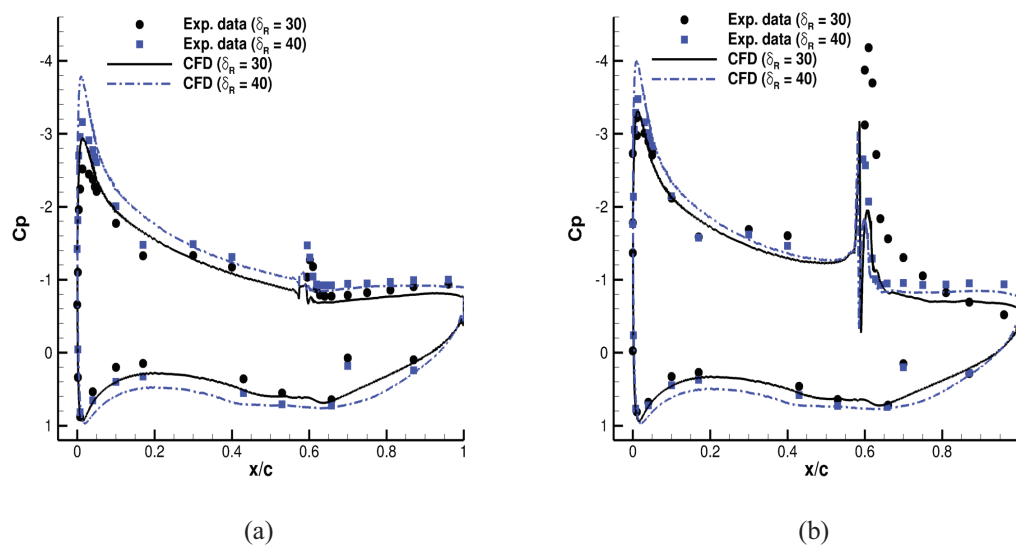


Figure 12. Effect of varying rudder deflection on chordwise pressures at $z/b = 70\%$ section, $\beta = 0^\circ$. (a) $C_{mu} = 0.0\%$ and (b) $C_{mu} = 0.5\%$.

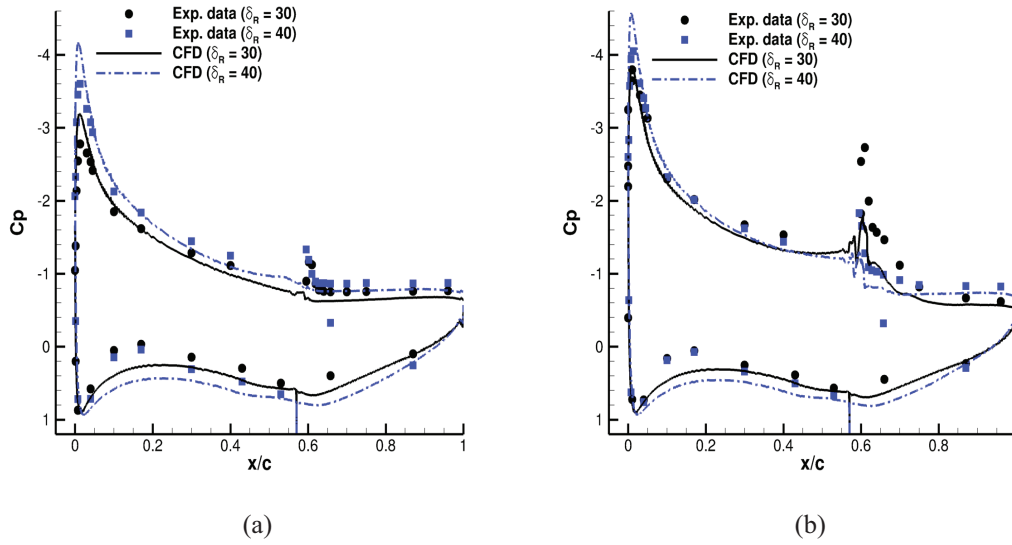


Figure 13. Effect of varying rudder deflection on chordwise pressures at $z/b = 89\%$ section, $\beta = 0^\circ$. (a) $C_{mu} = 0.0\%$ and (b) $C_{mu} = 0.5\%$.

5.3. Yaw Angle Variation, $\delta_R = 30^\circ$, $\beta = 7.5^\circ$

The next configuration under consideration was obtained from the baseline configuration by increasing the yaw angle, β from 0° to 7.5° . This yawed case corresponds to one of the configurations tested by Seele et al. [20]. The value of rudder deflection angle, δ_R , was kept at 30° for this series, which corresponds to the rudder deflection of the baseline configuration. Simulations have been performed at these rudder settings with $C_{mu} = 0$ and $C_{mu} = 0.5\%$. Once again, the time-averaging process was initiated after the integrated forces started settling in time.

The time-averaged pressure distributions for the 7.5° yaw angle at middle and outboard span stations are compared with the unyawed case in Figs. 14 and 15, respectively. The measured pressure distributions are also presented in these figures, along with the computational results for the baseline configuration ($\beta = 0^\circ$) for comparison purposes. The trends observed in the measured data due to yaw angle variation are replicated by the computational results for both the non-actuated and actuated cases. For example, the increase in suction peaks in the upstream region of the main element are

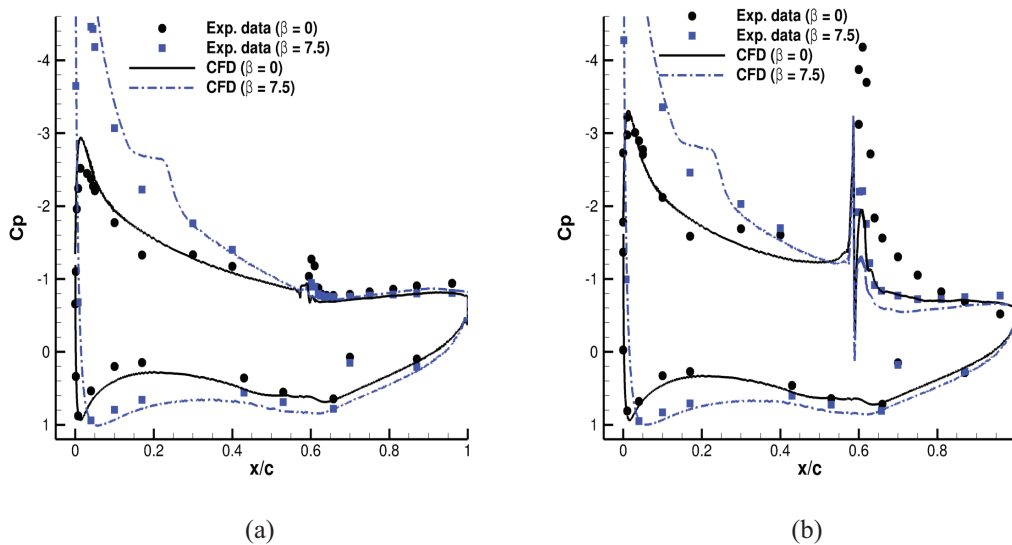


Figure 14. Effect of varying yaw angle on chordwise pressures at $z/b = 70\%$ section, $\delta_R = 30^\circ$. (a) $C_{mu} = 0.0\%$ and (b) $C_{mu} = 0.5\%$.

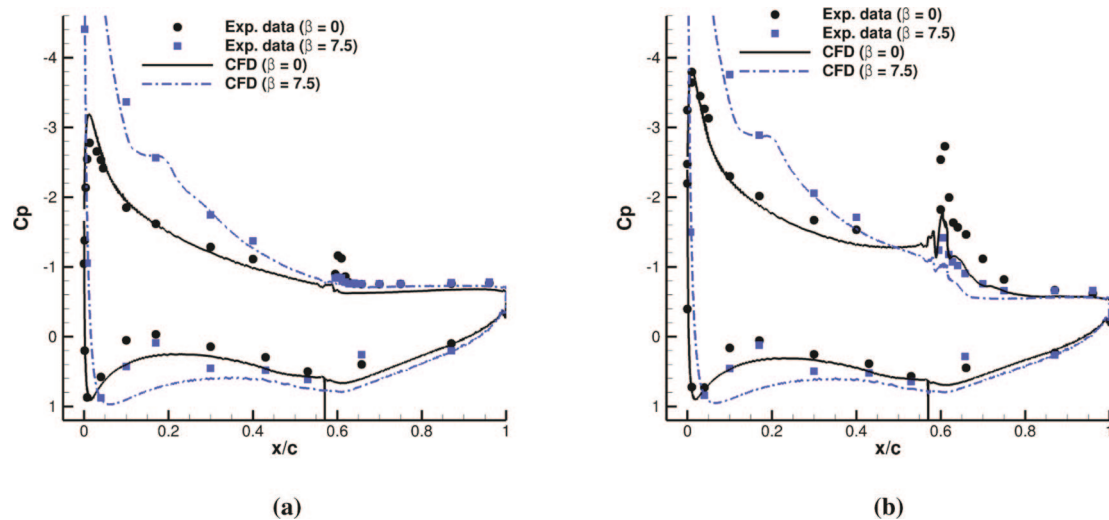


Figure 15. Effect of varying yaw angle on chordwise pressures at $z/b = 89\%$ section, $\delta_R = 30^\circ$. (a) $C_{mu} = 0.0\%$ and (b) $C_{mu} = 0.5\%$.

accurately predicted. A small pressure plateau near $x/c = 0.2$ is observed in the computed results for the yawed cases, a feature that may also be present in the measured data, but is not obvious due to sparseness of the experimental data. Another observation worth noting is the relatively flat C_p distribution in the aft region of rudder's suction surface, even for the case with actuation. Based on the pressure distributions, it is apparent that actuation with a momentum coefficient of $C_{mu} = 0.5\%$ was not adequate to control the flow separation for the yawed configuration.

The simulated surface streamline pattern for the yawed configuration are shown in Figs. 16 for the non-actuated and actuated cases, along with pressure contours. Looking at the pressure levels, it is clear that much higher suction pressure levels are obtained in the leading edge region of the main element over the entire span for both, the actuated and non-actuated cases, compared to the unyawed configuration (see Fig. 7). The streamline patterns shown in this figure indicate the presence of reverse flow region near leading edge of the main element for both, the actuated and non-actuated cases, a feature not observed for unyawed cases. For ease of visualization, separation and attachment lines are denoted on Fig. 16 (b). It is believed that the pressure plateau seen in Figs. 14 and 15 for $\beta = 7.5^\circ$ near $x/c = 0.2$ location of the main element is due to the presence of such reverse flow regions for the yawed cases.

5.4. High Reynolds Number, $Re_y = 23 \times 10^6$

The geometric parameters chosen for the next case correspond to the baseline rudder settings, i.e., a rudder deflection angle (δ_R) of 30° and a yaw angle (β) of 0° . However, the Reynolds number based on the mean aerodynamic chord of the main section was set to 23 million, which is typical for a vertical stabilizer in flight. Simulations have been performed for this configuration at $C_{mu} = 0$ and $C_{mu} = 0.5\%$, corresponding to the momentum coefficients used for the baseline configuration.

The time-averaged pressure distributions for this case at the middle and outboard span stations are compared with the baseline case in Figs. 17 and 18, respectively. Results for $C_{mu} = 0$ and $C_{mu} = 0.5\%$ are presented in these figures, along with the computational results and experimental data for the baseline case for comparison. Experimental data at the higher Reynolds number is currently not available for quantitative assessment at these conditions.

It is instructive to examine the trends in computational results due to increase in Reynolds number. For example, the increase in suction peaks in the leading-edge region of the main element for the non-actuated case due to increase in Reynolds number are comparable to what was observed by increasing the rudder deflection angle from $\delta = 30^\circ$ to $\delta = 40^\circ$ (see Figs. 12 and 13). For the actuated case ($C_{mu} = 0.5\%$), a much larger increase is observed in pressure levels on the suction surface, which in turn produces higher side force (see Table 2) with increase in Reynolds number. A reduction in the drag coefficient is also observed for the higher Reynolds number case. Similar trends in forces due to increase

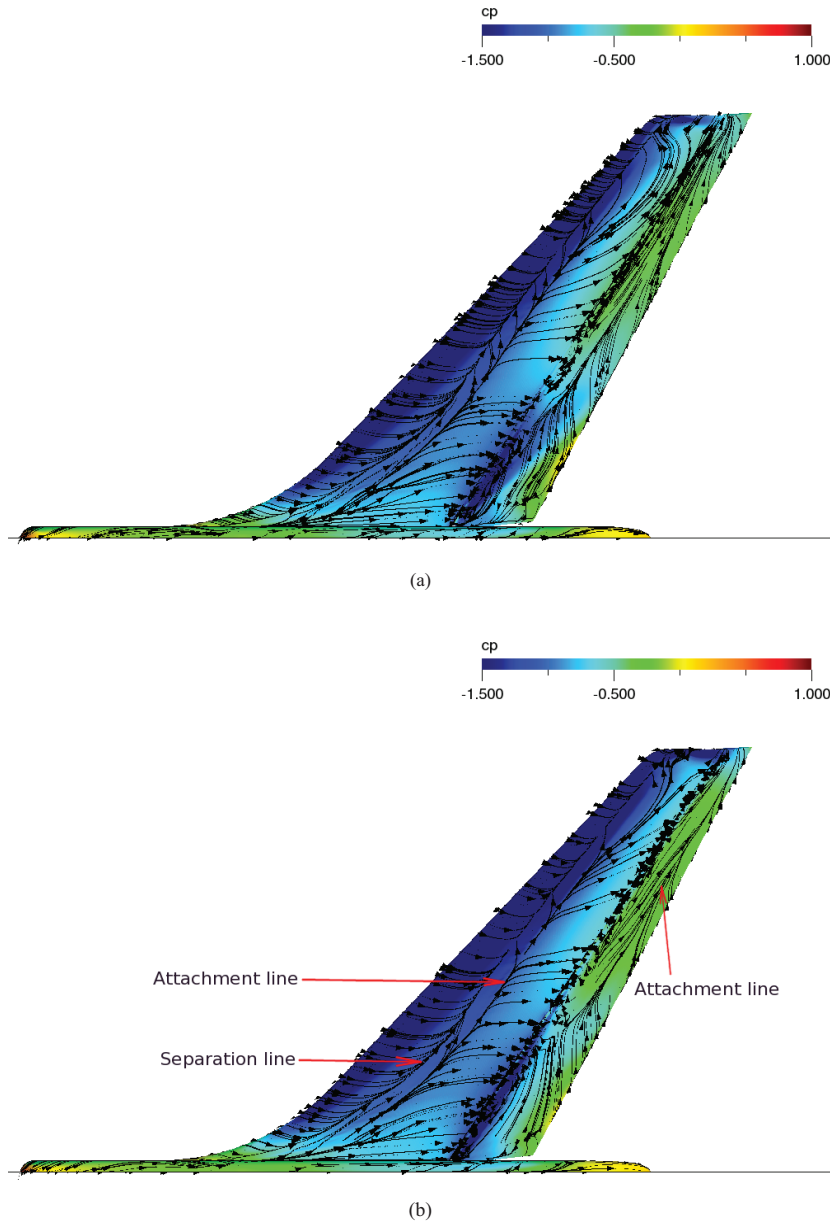


Figure 16. Effect of actuation on simulated suction surface streamlines, $\delta_R = 30^\circ$, $\beta = 7.5^\circ$. (a) $C_{\mu} = 0.0\%$ and (b) $C_{\mu} = 0.5\%$.

in Reynolds number were observed by Konig et al. [40] for a high-lift configuration. Based on these results, it appears that fluidic actuators have the potential to significantly enhance the performance of vertical stabilizers under flight conditions.

5.5. Flow Structure Inside the Actuator

An instantaneous view of the velocity magnitude field for one of the actuators is presented in Fig. 19. The oscillatory micro-jets issued from the actuator nozzle can be seen merging with the flow over the rudder in the vicinity of actuator exits. These frames were generated using the instantaneous velocity field at two different time instances to demonstrate the sweeping (oscillating) nature of the jets. The flow inside the actuator in Fig. 19 (a) appears to be leaning towards the right side of the section, whereas the flow at a later time (Fig. 19 (b)) is leaning the other way. We believe that the ability of fluidic actuators to produce sweeping jets oscillating in spanwise direction, which can energize much larger flow regions compared to steady jets issuing from same nozzles supplied with identical mass

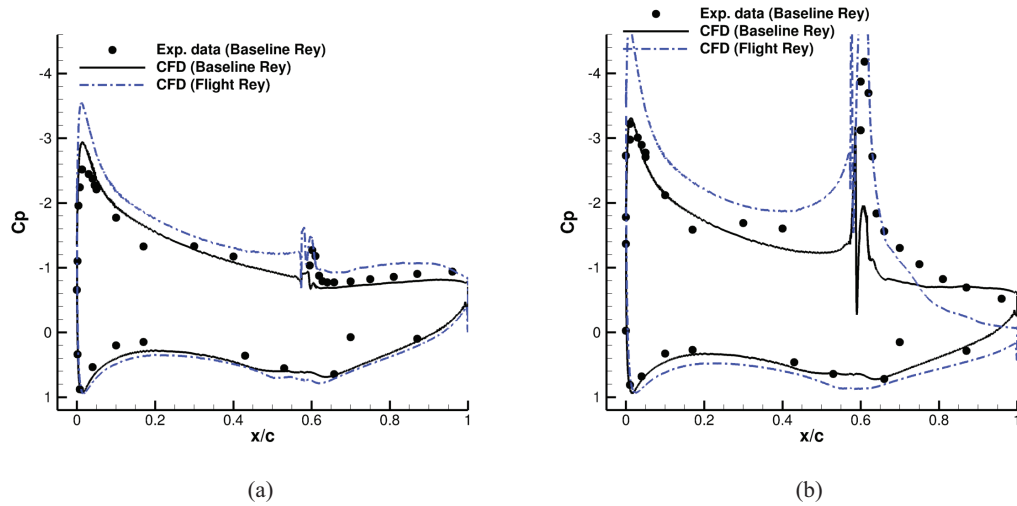


Figure 17. Effect of varying Reynolds number on chordwise pressures at $z/b = 70\%$ section, $\delta_R = 30^\circ$, $\beta = 0^\circ$. (a) $C_{mu} = 0.0\%$ and (b) $C_{mu} = 0.5\%$.

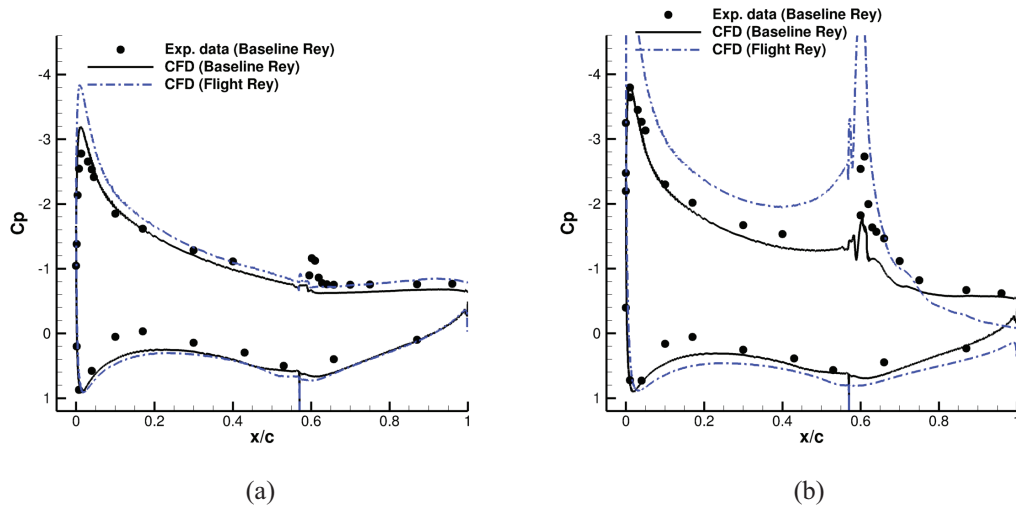


Figure 18. Effect of varying Reynolds number on chordwise pressures at $z/b = 89\%$ section, $\delta_R = 30^\circ$, $\beta = 0^\circ$. (a) $C_{mu} = 0.0\%$ and (b) $C_{mu} = 0.5\%$.

Table 2. Effect of Reynolds number on force coefficients

$\delta_R(deg)$	$\beta(deg)$	$C_{mu}(\%)$	$Rey \times 10^{-6}$	$C_Y (exp)$	$C_Y (CFD)$	$C_D (exp)$	$C_D (CFD)$
30.0	0.0	0.0	1.36	0.780	0.8540	0.112	0.1019
30.0	0.0	0.0	23.00	n.a.	0.9607	n.a.	0.1002
30.0	0.0	0.5	1.36	0.919	0.9273	0.106	0.0942
30.0	0.0	0.5	23.00	n.a.	1.1543	n.a.	0.0870

flow rates, contributes to the higher efficiency of these devices for flow control applications, as observed independently in various experimental studies [23–25].

5.6. Flow Characterization of Oscillating Micro-jets

To get a better understanding of the flow characteristics of oscillating jets produced by the fluidic actuators, the unsteady data generated during the simulation of the baseline configuration ($\delta_R = 30^\circ$, $\beta = 0^\circ$) with $C_{mu} = 0.5\%$ is examined in this section. The unsteady data collected at the center

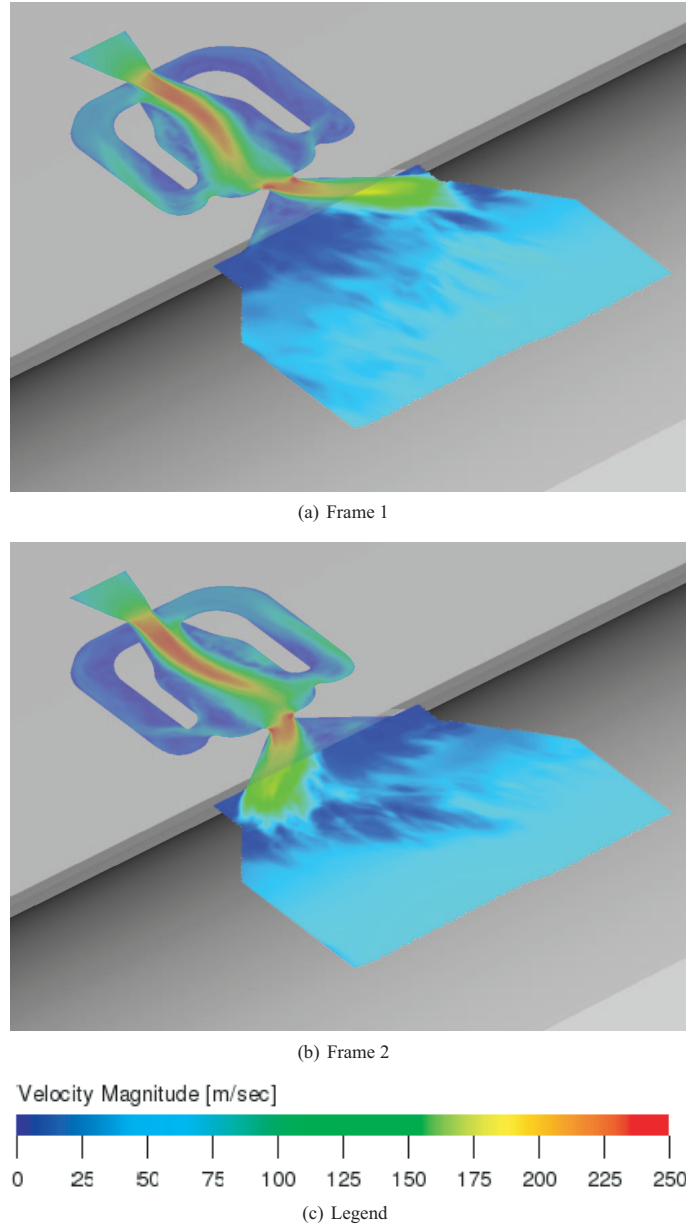


Figure 19. Velocity contours for actuator # 7 at two different times, baseline configuration.

of each actuator exit nozzle was analyzed to produce time-averaged mean, as well as standard and maximum deviation of Mach number and pressure. These results are shown in Fig. 20 for all 32 actuators. Even though all of the actuators were supplied air from a single feed tube, some variation is observed in flow properties for different actuators, especially in maximum deviation. The time-averaged Mach number and pressure are relatively constant along the span, implying a fairly uniform distribution of mass flow through the actuators. Mean deviation is also quite uniform across the span, but maximum deviation in both of these quantities is much larger and oscillatory in nature. For example, the average Mach number is about 0.22 and the maximum deviation in Mach number from its mean varies from 0.63 to 0.73. The occasional high velocity spikes inside the actuators result in space/time limited violations of LBM dynamic range that will be examined in future work.

The Power Spectral Density (PSD) map of pressure fluctuations at the actuator outlets is shown in Fig. 21 (a). Narrow peaks in PSD are observed at harmonic frequencies of about 1.6 kHz, the most dominant peak being at about 3.2 kHz. A slight variation in PSD levels for different actuators

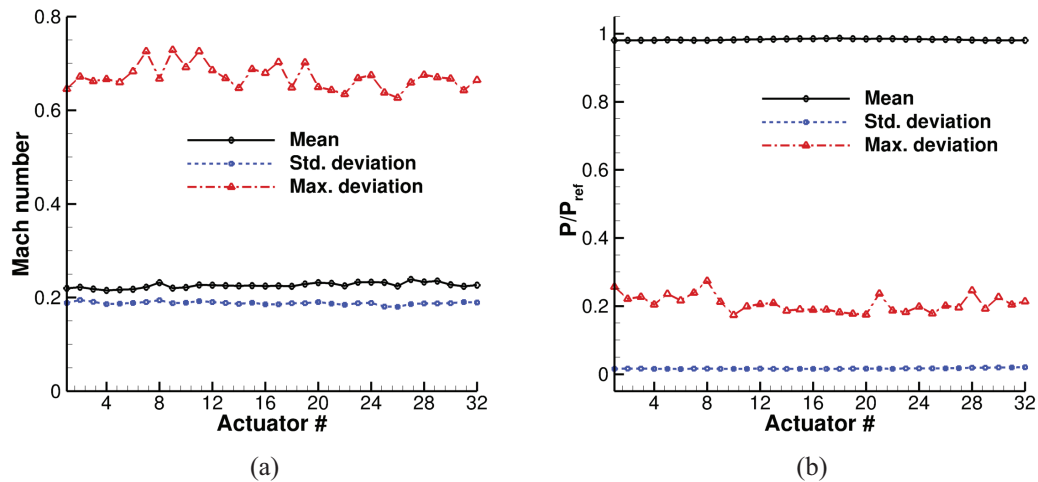


Figure 20. Spanwise variation in flow properties at the center of actuator exit nozzles. (a) Mach number and (b) pressure.

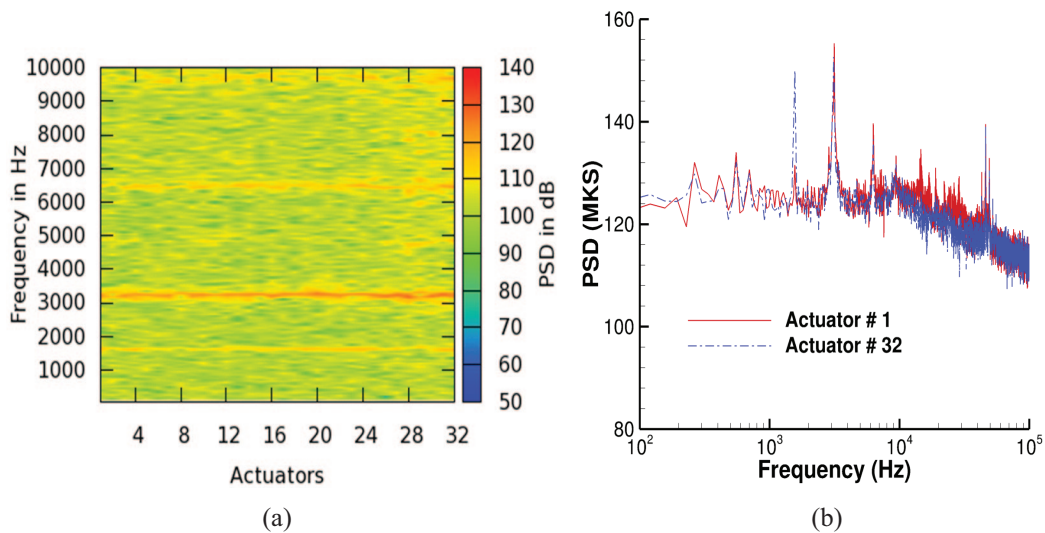


Figure 21. Power spectral density of pressure fluctuations at the center of actuator exit nozzles. (a) Spanwise map of PSD levels and (b) PSD comparison at root and tip sections.

is apparent from this figure. Such differences are more obvious in Fig. 21 (b), where the PSD levels for the innermost (# 1) and outermost (# 32) actuators are plotted as a function of frequency. The sharp peaks in PSD levels are observed at a frequency of about 1.6 kHz, and its harmonics, especially at 3.2 kHz. There are significant differences in dominant peak levels for these two actuators, which is most probably due to the differences in unsteady pressure perturbation deviations observed in Fig. 20 (b). Such differences in PSD levels will produce different acoustic signature. Other than these differences in peaks, the overall PSD levels for these actuators are very similar in nature.

Further analysis of the unsteady data was performed to determine whether the fluctuations induced by different actuators exhibit a mutual correlation, since these actuators are connected to a single feeding tube, and hence a certain acoustic coupling is expected. Fig. 22 (a) shows the maximum coherence between each pair of actuators for the baseline actuated case, where a regular pattern is observed. However, if we examine the map of the phase of the cross-spectrum in Fig. 22 (b), the phase lag corresponding to the peak value of the cross-spectrum is quite randomly distributed. Hence, it seems that the fluctuations in different actuators undergo a certain linear correlation, but they do not exhibit any phase locking behavior.

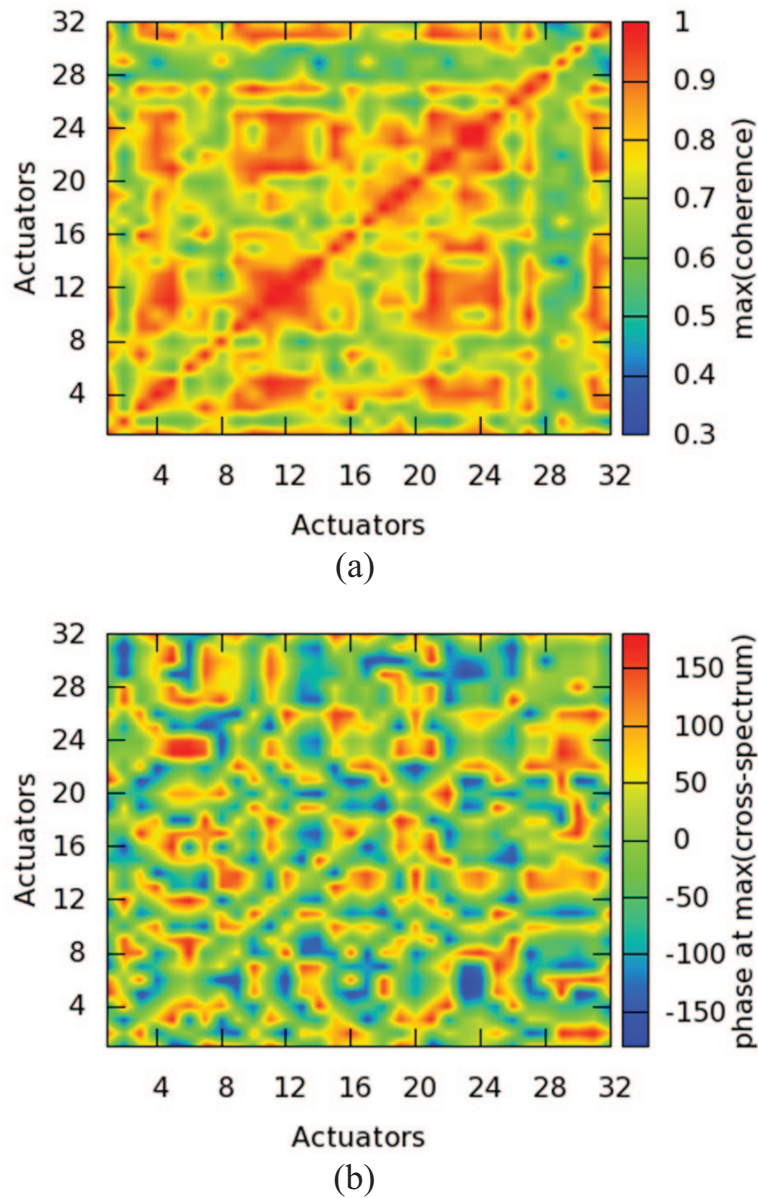


Figure 22. Coherence and phase angle characteristics of the fluidic actuators.
(a) maximum coherence and (b) phase angle.

6. CONCLUDING REMARKS

Numerical simulations have been performed using the PowerFLOW[®] CFD code for a vertical tail configuration with deflected rudder. This configuration has an array of fluidic actuators embedded on the suction surface of the main element in proximity of the trailing edge. Such actuators have been found to be very effective for flow control applications in the past. In the current approach, the entire flow field associated with this configuration, including the flow inside the actuators is simulated. The resulting solutions for force coefficients and surface pressure distributions are compared with available experimental data for several rudder settings simulated with and without actuation. Reasonably good agreement is obtained with the measured data for the baseline configuration ($\delta_R = 30^\circ$, $\beta = 0^\circ$), and simulated results predict the correct qualitative trends in forces with active flow control at these settings. However, the simulations under-predicted the increase in side force due to actuation compared to the experimentally measured levels.

Effect of varying yaw and rudder deflection angles are also examined in this paper, and simulations are shown to predict the experimentally observed trends in integrated forces and surface pressure

distributions. Even though the experimental data is available only at moderate wind tunnel Reynolds numbers, results from computations performed at a higher Reynolds number typical of flight conditions are also presented here to assess the performance of fluidic actuators at representative flight conditions. Significant increase in side force coefficient is predicted at higher Reynolds number with actuation, thus demonstrating the effectiveness of fluidic actuators at flight conditions.

Unsteady characteristics of oscillatory micro-jets issuing from the fluidic actuators have also been presented here. Although the mean flow properties at actuator exits are fairly uniform across the span, noticeable differences are observed in maximum deviation in unsteady Mach number and pressure levels. Similar differences are also observed in power spectral density distributions. Finally, it appears that the unsteady fluctuations in oscillatory micro-jets do not exhibit any phase locking behavior, even though all of the actuators are connected to the same feeding tube of constant cross-section.

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NOMENCLATURE

AFC	active flow control
A_{nozzle}	total exit area of all actuators
A_{ref}	total projected area of entire vertical stabilizer model
b	semi-span
CFD	computational fluid dynamics
C_D	drag coefficient, $F_x / (0.5 \rho_\infty V_\infty^2 A_{ref})$
C_Y	side-force coefficient, $F_y / (0.5 \rho_\infty V_\infty^2 A_{ref})$
C_{Y_0}	side-force coefficient for non-actuated case
C_{mu}	momentum coefficient, $\frac{A_{nozzle}}{2 * A_{ref}} * \left(\frac{V_j}{V_\infty} \right)^2$
C_p	pressure coefficient, $(p - p_\infty) / (0.5 \rho_\infty V_\infty^2)$
c	chord
DDES	delayed detached eddy simulation
DNS	direct numerical simulation
deg	degrees
exp	experimental
ERA	Environmentally Responsible Aviation
F_x, F_y	x, y components of integrated force on vertical stabilizer
k	turbulence kinetic energy
kg	kilogram
LBM	lattice Boltzmann model
lbm	pound mass
MAC	mean aerodynamic chord
m	meters
NASA	National Aeronautics and Space Administration
PSD	Power spectral density
Rey	Reynolds number based on mean aerodynamic chord
t	time
s, sec	seconds
VR	variable resolution regions
3-D	three-dimensional
u, v, w	Cartesian fluid velocity components

x, y, z	Cartesian coordinates
δ_R	rudder deflection angle
β	yaw angle
ρ	density
ϵ	dissipation length scale for turbulence model

Superscript:

o	degree
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Subscript:

j	jet exit quantity
∞	free-stream quantity

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